# Optimization in Allocating Goods to Shop Shelves Under the Utilization of Genetic Algorithm With Sales Probabilities 

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#### Abstract

How to allocate goods in shop shelves makes great influence to sales amount．Searching best fit allocation of goods to shelves is a kind of combinatorial problem．This becomes a problem of integer programming and utilizing genetic algorithm may be an effective method．Reviewing past researches， there are few researches made on this．Formerly，we have presented a papers concerning optimization in allocating goods to shop shelves utilizing genetic algorithm．In those papers，the problem that goods were not allowed to allocate in multiple shelves and the problem that goods were allowed to allocate in multiple shelves were pursued．In this paper，the problem that allows goods to be allocated in multiple shelves is examined and the concept of sales profits and sales probabilities are introduced．Optimization in allocating goods to shop shelves is investigated．Problem description is executed．Utilizing genetic algorithm，optimum solution is pursued and verified by a simple numerical example．Various patterns of problems must be examined hereafter．


Keywords：display，genetic algorithm，optimization，shelf

## 1．INTRODUCTION

Displaying method in the shop makes influence to sales amount，therefore various ideas are devised． What kind of items should be placed where in the shop，how to guide customers to what aisle in the shop are the big issues to be discussed．Searching best fit allocation of goods to shelves is also an important issue to be solved．In this paper，we seek how to optimize in allocating goods to shop shelves．

As for allocating good to shop shelves，following items are well known（Nagashima，2005）．

Shelf height is classified as follows．
－Shelf of 135 cm height：Customers can see the whole space of the shop．Specialty stores often use this type．
－Shelf of 150 cm height：Female customers may feel pressure to the shelf height．This height may be the upper limit to look over the shop．
－Shelf of 180 cm height：It becomes hard to look over the shop．Therefore it should not be used for island display（display at the center or inside the shop）．

Next，we show the following three functions of shelf for display．

1．Exhibition of goods function

2．Stock function
3．Display function
Effective range for exhibition is generally said to be $45 \mathrm{~cm}-150 \mathrm{~cm}$ ．The range of $75 \mathrm{~cm}-135 \mathrm{~cm}$ is called golden zone especially．For the lower part under 45 cm ，goods are stocked as well as displaying．

Reviewing past papers，there are many papers concerning lay out problem．As for the problem of the distribution of equipment，we can see B．Korte et al． （2005），M．Gen et al．（1997）for the general research book．There are many researches made on this． Yamada et al．（2004）handles the lay out problem considering the aisle structure and intra－department material flow．Y．Wu et al．（2002）and Yamada et al． （2004）handle this problem considering aisle structure． Ito et al．（2006）considers multi－floor facility problem．

Although there are many researches on corresponding theme as stated above，we can hardly find researches on the problem of optimization in allocating goods to shop shelves．

Formerly，we have presented a paper concerning optimization in allocating goods to shop shelves utilizing genetic algorithm（Takeyasu et al．，2008）．In those papers，the problem that goods were not allowed
to allocate in multiple shelves and the problem that goods were allowed to allocate in multiple shelves were pursued. In this paper, the problem that allows goods to be allocated in multiple shelves is examined and the concept of sales profits and sales probabilities are introduced. Optimization in allocating goods to shop shelves is investigated. Problem description is executed. Utilizing genetic algorithm, optimum solution is pursued and verified by a simple numerical example.

The rest of the paper is organized as follows. Problem description is stated in section 2. Genetic Algorithm is developed in section 3. Numerical example is exhibited in section 4 which is followed by the remarks of section 5 . Section 6 is a summary.

## 2. PROBLEM DESCRIPTION

Shelf model is constructed as Figure 1. There are five shelf positions. Shelf position 1 is mainly to put big and heavy goods including stock function. Shelf position 3, 4 at the height of the range 75 cm to 135 cm are the space of golden zone. Thus, we can use shelves properly by assuming these shelves. In numerical example, we examine using these five shelves. First of all, we make problem description in the case there is only one shelf (case 1). Then we expand to the case there are multiple shelves (case 2).


Figure 1: Shelf Model
(1) Case 1: The case that there is only one shelf

Although there are few cases that there is only one shelf, it makes the foundation for multiple shelves case. Therefore we pick it up as a fundamental one. Suppose shelf position $k$ is from 1 to $L$ (Figure 2).

| $k=L$ |
| :---: |
| $\vdots$ |
| $k=3$ |
| $k=2$ |
| $k=1$ |

Figure 2: Shelf Position

Suppose there are $N$ amount of goods $(i=1, \cdots, N)$. Set sales profit of goods $i$ as $H^{i}$.
Table 1 shows the sales probabilities when each goods is placed at each shelf position. The values in this table are written for example.

Table 1: Sales probability for each goods

| Day of the Week | Time Zone ( $t$ ) | Shelf $j=1$ |  |  | Shelf $j=2$ |  |  | ... | Shelf $j=m$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Shelf Position |  |  | Shelf Position |  |  | ... | Shelf Position |  |  |
|  |  | $k=1$ | ... | $k=L_{1}$ | $k=1$ | ... | $k=L_{2}$ | $\ldots$ | $k=1$ | . | $k=L_{m}$ |
| (Mon.) | $0-1(t=1)$ | 0.01 | ... |  |  |  |  |  |  |  |  |
|  | $1-2(t=2)$ | 0.02 |  |  |  |  |  |  |  |  |  |
|  | ... |  |  |  |  |  |  |  |  |  |  |
|  | $23-24(t=24)$ | 0.03 |  |  |  |  |  |  |  |  |  |
| (Tue.) | $0-1(t=25)$ | 0.02 |  |  |  |  |  |  |  |  |  |
|  | $1-2(t=26)$ | 0.02 |  |  |  |  |  |  |  |  |  |
|  | ... |  |  |  |  |  |  |  |  |  |  |
|  | $23-24(t=48)$ | 0.03 |  |  |  |  |  |  |  |  |  |
| ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| (Sun.) | $0-1(t=145)$ | 0.02 |  |  |  |  |  |  |  |  |  |
|  | $1-2(t=146)$ | 0.03 |  |  |  |  |  |  |  |  |  |
|  | ... |  |  |  |  |  |  |  |  |  |  |
|  | $23-24(t=168)$ | 0.04 |  |  |  |  |  |  |  |  |  |

Suppose goods are sold in the period from $t_{1}$ to $t_{n}$. In addition, a new goods $i$ is replenished when goods $i$ is sold out.

Set the accumulated sales probability of goods $i$ in time zone $t$, shelf $j$, and shelf position $k$ in the table as $H K_{t, j, k}^{i}$.

Then, the sales probability $K_{t_{1} / t_{n}}^{i, j}$ of goods $i$ in the period will be described as follows.
$K_{t_{1} / t_{n}}^{i, j}=\sum_{t=1}^{n} H K_{t, j, k}^{i}$
This can take the value more than 1. For example, the value 2 means that 2 amount of goods were sold during the period.

Set Benefit in the sales period from $t_{1}$ to $t_{n}$ as $P_{t_{1} / t_{n}}^{i, j, k}(i=1, \cdots, N)(j=1, \cdots, m)(k=1, \cdots, L)$ when goods $i$ is placed at shelf $j$ and shelf position $k$. Where Benefit means:

## Benefit $=$ SalesProbability $\times$ SalesProfit

Therefore, this equation is represented as follows.

$$
\begin{equation*}
P_{t_{1} / t_{n}}^{i, j, k}=K_{t_{1} / t_{n}}^{i, j, k} \cdot H^{i} \tag{1}
\end{equation*}
$$

where $j=1$ because one shelf case is considered here.

Set $x_{i, k}$ as:
$x_{i, k}=1:$ Goods $i$ is placed at shelf position $k$.

$$
x_{i, k}=0: \text { Else }
$$

Suppose only one goods can be placed at one shelf position and also suppose that goods is allowed to allocate in multiple shelf positions. Then constraints are described as follows.

$$
\begin{align*}
& x_{i, k}=1,0(i=1, \cdots, N)(k=1, \cdots, L)  \tag{2}\\
& \sum_{i=1}^{N} x_{i, k}=1(k=1, \cdots, L) \tag{3}
\end{align*}
$$

Under these constraints,

$$
\begin{equation*}
J=\sum_{k=1}^{L} \sum_{i=1}^{N} P_{t_{1} / t_{n}}^{i, j, k} x_{i, k} \rightarrow \operatorname{Max} \tag{4}
\end{equation*}
$$

(2) Case 2: The case that there are $m$ shelves

Suppose there are $m$ shelves (Figure 3). Set Benefit as $P_{t_{1} / t_{n}}^{i, j, k}(i=1, \cdots, N),(j=1, \cdots, m),\left(k=1, \cdots, L_{j}\right)$ where goods $i$ is placed at shelf position $k$ of shelf $j$. The sales period is the same with above stated (1).

Figure 3: Shelf Position under multiple shelves

Set $x_{i, j, k}$ as:
$x_{i, j, k}=1:$ Goods is placed at shelf position $k$ of shelf $j$ $x_{i, j, k}=0:$ Else

Suppose only one goods can be placed at one shelf position and also suppose that goods is allowed to allocate in multiple shelf positions. Then constraints are described as follows. The sales period is the same with before.

$$
\begin{align*}
& x_{i, j, k}=1,0(i=1, \cdots, N)(j=1, \cdots, m) \\
& \left(k=1, \cdots, L_{j}\right)  \tag{5}\\
& \sum_{i=1}^{N} x_{i, j, k}=1(j=1, \cdots, m)\left(k=1, \cdots, L_{j}\right) \tag{6}
\end{align*}
$$

Under these constraints,

$$
\begin{equation*}
J=\sum_{i=1}^{N} \sum_{j=1}^{m} \sum_{k=1}^{L_{j}} P_{t_{1} / t_{n}}^{i, j, k} x_{i, j, k} \rightarrow \operatorname{Max} \tag{7}
\end{equation*}
$$

## 3. ALGORITHM

We can make problem description as stated above, although these are somewhat under restricted cases. As far as only these are considered as they are, there is little difference between these and the conventional optimization problems. However, as soon as the number of involved shelves becomes larger, the number of variables dramatically grows greater, to which the application of Genetic Algorithm solution and Neural Network solutions may be appropriate. There are various means to solve this problem. When that variable takes the value of 0 or 1 , the application of genetic algorithm would be a good method. As is well known, the calculation volume reaches numerous or even infinite amounts in these problems when the number of variables increases. It is reported that GA is effective for these problems (Gen et al. (1995), Lin et al. (2005), Zhang et al. (2005)).

## A. The Variables

Suppose the number of goods, shelf position, and shelf are $20,5,2$ respectively. Then the number of variables becomes two hundred.

$$
x_{i, j, k}=1,0(i=1, \cdots, 20)(j=1,2)(k=1, \cdots, 5)
$$

Therefore, set chromosome as follows.

$$
\begin{align*}
X & =\left(x_{1,1,1}, x_{2,1,1}, x_{3,1,1}, \cdots, x_{20,1,1}\right. \\
& x_{1,1,2}, x_{2,1,2}, x_{3,1,2}, \cdots, x_{20,1,2} \\
& \vdots \\
& x_{1,1,5}, x_{2,1,5}, x_{3,1,5}, \cdots, x_{20,1,5}  \tag{8}\\
& x_{1,2,1}, x_{2,2,1}, x_{3,2,1}, \cdots x_{20,2,1} \\
& x_{1,2,2}, x_{2,2,2}, x_{3,2,2}, \cdots, x_{20,2,2} \\
& \vdots \\
& \left.x_{1,2,5}, x_{2,2,5}, x_{3,2,5}, \cdots, x_{20,2,5}\right)
\end{align*}
$$

## B. Initialize population

Initialization of population is executed. The number of initial population is $M$. Here set $M=100$. Set gene at random and choose individual which satisfies constraints.

## C. Selection

In this paper, we take elitism while selecting. Choose $P$ individuals in the order which take maximum score of objective function.
Here, set $P=20$

## D. Crossover

Here, we take uniform crossover.
Set crossover rate as:

$$
\begin{equation*}
P_{c}=0.7 \tag{9}
\end{equation*}
$$

## E. Mutation

Set mutation rate as:

$$
\begin{equation*}
P_{m}=0.01 \tag{10}
\end{equation*}
$$

Algorithm of GA is exhibited at Table 2.

Table 2: Algorithm of multi-step tournament selection method

Step 1: Set maximum No. as $g_{\text {max }}$, population size as $P$, crossover rate as $p_{c}$, mutation rate as $p_{m}$.
Step 2: Set $t=1$ for generation No. and generate initial solution matrix $\quad x_{p}(t)=\left(x_{i, j, k}^{p}\right)$ $(p=1, \cdots, M)$.
Step 3 : Calculate Objective function $J\left(x_{p}(t)\right)$ for all solution matrix $x_{p}(t) \quad(p=1, \cdots, P)$ in generation $t$.
Step 4: Set $t=t+1$ until $t>g_{\text {max }}$.
Step 5 : Crossover
Generate new individual by crossover utilizing the method of above stated $D$.
Step 6 : Mutation
Reproduce by mutation utilizing the method of above stated $E$.
Step 7: Calculate objective function for reproduction of generation $t$.
Step 8 : Selection
Next generation is selected by elitism. Go to Step 4.

Introducing the variable $y_{s}$ such that:

$$
\begin{equation*}
y_{s}=i \tag{11}
\end{equation*}
$$

where

$$
\begin{equation*}
s=k+(j-1) \cdot 5 \tag{12}
\end{equation*}
$$

when

$$
x_{i, j, k}=1
$$

then (8) is expressed as:

$$
\begin{equation*}
Y=\left(y_{1}, y_{2}, \cdots, y_{10}\right) \tag{13}
\end{equation*}
$$

## 4. NUMERICAL EXAMPLE

Now, we execute numerical example. Numerical example is executed in "Case 2" of 2 (2). Suppose the sales period is 3 days for Thursday, Friday, and Saturday. Table 3 shows the sales profit $H^{i}$ of each goods.

Table 3: Sales Profit of each goods

| Lot $i$ | $H^{i}$ |
| :---: | :---: |
| 1 | 6000 |
| 2 | 5500 |
| 3 | 5500 |
| 4 | 5000 |
| 5 | 4500 |
| 6 | 4500 |
| 7 | 4000 |
| 8 | 3500 |
| 9 | 3000 |
| 10 | 3000 |
| 11 | 6000 |
| 12 | 5500 |
| 13 | 5000 |
| 14 | 4500 |
| 15 | 4000 |
| 16 | 3500 |
| 17 | 3000 |
| 18 | 4000 |
| 19 | 3000 |
| 20 | 2000 |

For Women

For Men

For Kids

Supposing a general daytime retail store, we set opening time to be 10 through 20 o'clock. Table 4 shows the sales probabilities of lot 5 as an example.

Table 4: Sales Probabilities of Lot 5

| Day <br> of the <br> Week | Time Zone ( $t$ ) | Shelf $j=1$ |  |  |  |  | Shelf $j=2$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Shelf Position |  |  |  |  | Shelf Position |  |  |  |  |
|  |  | $k=1$ | $k=2$ | $k=3$ | $k=4$ | $k=5$ | $k=1$ | $k=2$ | $k=3$ | $k=4$ | $k=5$ |
| (Thu.) | 10-11 | 0.01 | 0.02 | 0.03 | 0.04 | 0.03 | 0.02 | 0.04 | 0.05 | 0.05 | 0.04 |
|  | 11-12 | 0.02 | 0.03 | 0.04 | 0.05 | 0.04 | 0.03 | 0.05 | 0.06 | 0.06 | 0.05 |
|  | 12-13 | 0.01 | 0.03 | 0.05 | 0.04 | 0.03 | 0.02 | 0.05 | 0.05 | 0.05 | 0.04 |
|  | 13-14 | 0.02 | 0.03 | 0.05 | 0.04 | 0.03 | 0.03 | 0.05 | 0.06 | 0.05 | 0.05 |
|  | 14-15 | 0.02 | 0.03 | 0.05 | 0.05 | 0.04 | 0.03 | 0.05 | 0.06 | 0.06 | 0.05 |
|  | 15-16 | 0.03 | 0.04 | 0.04 | 0.05 | 0.04 | 0.03 | 0.04 | 0.07 | 0.07 | 0.06 |
|  | 16-17 | 0.03 | 0.05 | 0.05 | 0.06 | 0.04 | 0.03 | 0.04 | 0.07 | 0.06 | 0.04 |
|  | 17-18 | 0.03 | 0.04 | 0.04 | 0.03 | 0.03 | 0.02 | 0.04 | 0.06 | 0.06 | 0.03 |
|  | 18-19 | 0.02 | 0.04 | 0.05 | 0.04 | 0.04 | 0.02 | 0.04 | 0.06 | 0.05 | 0.05 |
|  | 19-20 | 0.02 | 0.03 | 0.06 | 0.05 | 0.04 | 0.03 | 0.05 | 0.05 | 0.05 | 0.04 |
| (Fri.) | 10-11 | 0.01 | 0.02 | 0.03 | 0.03 | 0.02 | 0.02 | 0.03 | 0.04 | 0.04 | 0.03 |
|  | 11-12 | 0.01 | 0.02 | 0.04 | 0.03 | 0.02 | 0.01 | 0.04 | 0.05 | 0.04 | 0.03 |
|  | 12-13 | 0.02 | 0.03 | 0.04 | 0.04 | 0.03 | 0.02 | 0.04 | 0.05 | 0.05 | 0.04 |
|  | 13-14 | 0.02 | 0.04 | 0.04 | 0.04 | 0.03 | 0.03 | 0.05 | 0.04 | 0.05 | 0.05 |
|  | 14-15 | 0.03 | 0.04 | 0.05 | 0.06 | 0.04 | 0.03 | 0.05 | 0.05 | 0.04 | 0.05 |
|  | 15-16 | 0.03 | 0.04 | 0.05 | 0.05 | 0.04 | 0.03 | 0.06 | 0.05 | 0.06 | 0.06 |
|  | 16-17 | 0.03 | 0.05 | 0.05 | 0.05 | 0.04 | 0.04 | 0.06 | 0.06 | 0.06 | 0.05 |
|  | 17-18 | 0.04 | 0.05 | 0.06 | 0.06 | 0.05 | 0.04 | 0.05 | 0.06 | 0.06 | 0.06 |
|  | 18-19 | 0.02 | 0.04 | 0.06 | 0.05 | 0.04 | 0.04 | 0.06 | 0.07 | 0.05 | 0.06 |
|  | 19-20 | 0.02 | 0.05 | 0.06 | 0.05 | 0.05 | 0.03 | 0.06 | 0.07 | 0.06 | 0.05 |
| (Sat.) | 10-11 | 0.02 | 0.02 | 0.03 | 0.02 | 0.02 | 0.02 | 0.03 | 0.04 | 0.04 | 0.04 |
|  | 11-12 | 0.03 | 0.02 | 0.04 | 0.03 | 0.02 | 0.03 | 0.04 | 0.04 | 0.05 | 0.04 |
|  | 12-13 | 0.03 | 0.03 | 0.06 | 0.04 | 0.04 | 0.04 | 0.06 | 0.06 | 0.05 | 0.04 |
|  | 13-14 | 0.03 | 0.04 | 0.07 | 0.06 | 0.05 | 0.04 | 0.05 | 0.05 | 0.06 | 0.05 |
|  | 14-15 | 0.03 | 0.05 | 0.07 | 0.06 | 0.05 | 0.04 | 0.06 | 0.06 | 0.06 | 0.05 |
|  | 15-16 | 0.04 | 0.05 | 0.05 | 0.06 | 0.05 | 0.04 | 0.06 | 0.07 | 0.07 | 0.06 |
|  | 16-17 | 0.04 | 0.05 | 0.06 | 0.05 | 0.04 | 0.04 | 0.05 | 0.08 | 0.06 | 0.07 |
|  | 17-18 | 0.03 | 0.05 | 0.06 | 0.06 | 0.05 | 0.04 | 0.07 | 0.08 | 0.07 | 0.07 |
|  | 18-19 | 0.04 | 0.05 | 0.07 | 0.07 | 0.06 | 0.05 | 0.07 | 0.07 | 0.08 | 0.06 |
|  | 19-20 | 0.03 | 0.06 | 0.05 | 0.05 | 0.04 | 0.05 | 0.06 | 0.06 | 0.07 | 0.07 |

Table 5 shows the benefit when each goods is placed at each shelf position of each shelf.

Table 5: Benefit Table

|  | Shelf 1 |  |  |  |  | Shelf 2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Shelf Position |  |  |  |  | Shelf Position |  |  |  |  |
| Lot $i$ | 1 | 2 | 3 | 4 | 5 | 1 | 2 | 3 | 4 | 5 |
| 1 | 2580 | 4380 | 5400 | 5220 | 4380 | 5220 | 7020 | 7980 | 7800 | 7020 |
| 2 | 2750 | 4620 | 5610 | 5390 | 4620 | 5005 | 6820 | 7810 | 7590 | 6820 |
| 3 | 3025 | 4840 | 5830 | 5610 | 4840 | 4840 | 6600 | 7590 | 7425 | 6600 |
| 4 | 3200 | 5000 | 6000 | 5800 | 5000 | 4600 | 6400 | 7400 | 7200 | 6400 |
| 5 | 3420 | 5130 | 6750 | 6345 | 5130 | 4230 | 6750 | 7830 | 7560 | 6660 |
| 6 | 3600 | 5400 | 6390 | 6210 | 5400 | 4185 | 5985 | 7020 | 6795 | 5985 |
| 7 | 3800 | 5600 | 6600 | 6400 | 5600 | 4000 | 5800 | 6800 | 6600 | 5800 |
| 8 | 3990 | 5810 | 6790 | 6615 | 5810 | 3815 | 5600 | 6615 | 6405 | 5600 |
| 9 | 4200 | 6000 | 6900 | 6810 | 6000 | 3600 | 5400 | 6300 | 6210 | 5400 |
| 10 | 4410 | 6210 | 7200 | 6990 | 6210 | 3390 | 5190 | 6210 | 6000 | 5190 |
| 11 | 2220 | 4980 | 5820 | 6000 | 5580 | 4200 | 7020 | 7800 | 7980 | 7620 |
| 12 | 2420 | 5225 | 5995 | 6215 | 5830 | 4015 | 6820 | 7590 | 7810 | 7425 |
| 13 | 2600 | 5400 | 6200 | 6400 | 6000 | 3800 | 6600 | 7400 | 7600 | 7200 |
| 14 | 2790 | 5580 | 6390 | 6615 | 6210 | 3600 | 6390 | 7200 | 7380 | 7020 |
| 15 | 3000 | 5800 | 6600 | 6800 | 6400 | 3400 | 6200 | 7000 | 7200 | 6800 |
| For |  |  |  |  |  |  |  |  |  |  |
| Men |  |  |  |  |  |  |  |  |  |  |
| 16 | 3185 | 5985 | 6790 | 7000 | 6615 | 3185 | 5985 | 6790 | 7000 | 6615 |
| 17 | 3390 | 6240 | 6990 | 7200 | 6810 | 3000 | 5790 | 6600 | 6810 | 6390 |
| 18 | 6800 | 6800 | 3200 | 2400 | 200 | 8000 | 8000 | 4400 | 3400 | 1400 |
| 19 | 6990 | 6990 | 3390 | 2610 | 390 | 7800 | 7800 | 4200 | 3210 | 1200 |
| 20 | 7200 | 7200 | 3600 | 2800 | 600 | 7600 | 7600 | 4000 | 3000 | 1000 |

Experimental results are as follows. The expression Eq. (8) is complicated. Therefore we use expression by Eq. (13). A sample set of initial population is exhibited in Table 6.

Table 6: A Sample Set of Initial Population

| $Y_{1}=$ | ( | 7 | 20 | 2 | 9 | 9 | 5 | 19 | 5 | 17 | 14 | ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $Y_{2}=$ | ( | 11 | 14 | 4 | 13 | 11 | 16 | 11 | 3 | 5 | 18 | ) |
| $Y_{3}=$ | ( | 12 | 18 | 10 | 15 | 2 | 20 | 4 | 12 | 19 | 15 | ) |
| $Y_{98}=$ | ( | 11 | 2 | 6 | 12 | 20 | 12 | 18 | 16 | 9 | 9 | ) |
| $Y_{99}=$ | ( | 9 | 16 | 6 | 11 | 3 | 18 | 6 | 3 | 10 | 6 | ) |
| $Y_{100}=$ | ( | 8 | 12 | 4 | 17 | 15 | 12 | 13 | 7 | 14 | 2 | ) |

Convergence process is exhibited in Figure 4.


Figure 4: Convergence Process of Case 2

The problem is simple, so combination of genotype for crossover saturates in the 65 th generation. Genotype in which objective function becomes maximum is as follows.

$$
Y=(20,20,10,17,17,18,18,1,11,11)
$$

This coincides with the result of optimal solution by the calculation of all considerable cases, therefore it coincides with a theoretical optimal solution. We take up simple problem and we can confirm the effectiveness of GA approach. Further study for complex problems should be examined hereafter.

## 5. REMARKS

As there are few papers made on this theme, we constructed prototype version before (Takeyasu et al.,2008). In this paper, we examined the problem that allowed goods to be allocated in multiple shelves and introduced the concept of sales profits and sales probabilities. We can see that genetic algorithm is effective for this problem.

In practice, following themes occur.

1. Goods are made into groups and they are placed in the zone of specified multiple shelves.
2. There are various types of shelves corresponding to goods characteristics.
For these issues, expansion is easy to make. Expanded version of the paper will be built hereafter consecutively.

## 6. CONCLUSION

How to allocate goods in shop shelves makes great influence to sales amount. Searching best fit allocation of goods to shelves is a kind of combinatorial problem. This becomes a problem of integer programming and utilizing genetic algorithm may be an effective method. Reviewing past researches, there were few researches made on this. Formerly, we had presented papers concerning optimization in allocating goods to shop shelves utilizing genetic algorithm. In those papers, the problem that goods were not allowed to allocate in multiple shelves and the problem that goods were allowed to allocate in multiple shelves were pursued. In this paper, the problem that allows goods to be allocated in multiple shelves was examined and the concept of sales profits and sales probabilities were introduced. Optimization in allocating goods to shop shelves was investigated. Problem description was executed. Utilizing genetic algorithm, optimum solution was pursued and verified by a simple numerical example. Various patterns of problems should be examined hereafter.

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